Map: College Pre-calculus Type: Consensus Grade Level: 12 School Year: 2011-2012

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	Essential Questions	Content	Skills	Assessments	Standards/PIs	Resources/Notes
Unit 1	What are the alternate ways to perform long division?	Basic Concepts of Algebra	Evaluate Algebraic Expressions		MST3-A2.A.7	
	How is synthetic division relevant to the roots of an equation?	Algebra Review	Determine the Domain of a Variable Graph Inequalities		MST3-A2.A.8 MST3-A2.A.16	
		Factoring	Find Distance on the Real Number Line			
		Delynomials	Use the Law of Exponents Evaluate Square Roots			
		Polynomials	Recognize Special Products			
		<u>Vocabulary</u>	Factor Polynomials			
		domain, inequality, base, exponent, power, principal	Simplify Rational Expressions			
		square root, special products, LCM, divisor, dividend, quotient, remainder, synthetic	Use LCM to Add Rational Expressions			
		division	Divide Polynomials Using Long Division			
			Divide Polynomials Using Synthetic Division			
			Explain how to use long division and synthetic division.			
N	How is the quadratic	Equations and	Solve Linear Equations		MST3-A2.A.25	
Unit 2	formula connected to the graph of the function?	<u>Inequalities</u>		ī.	MST3-A2.A.26	
		Quadratic Equations	Solve Rational Equations		MST3-A2.N.6	
	How does interval notation help us?	Linear Equations/Inequalities with Absolute Value	Solve Quadratic Equations by Factoring		MST3-A2.N.7 MST3-A2.N.9	
	Why is dimensional analysis important?	Complex Numbers	Solve Quadratic Equations by Square Root Method			
		Proportion with applications to mixture problems, conversion, and dimensional	Solve Quadratic Equations by Completing the Square			
		analysis	Solve Quadratic Equations Using Quadratic Formula			

Radical Equations	Solve Equations Quadratic
	in Form
<u>Vocabulary</u>	
Square Root Method, completing the square, quadratic in form, closed interval, open interval, half- open interval, complex	Solve Absolute Value Equations
numbers, conjugate, interest, principal, rate of	Solve Eqations by Factoring
interest, simple interest, mixture problems, uniform	Use Interval Notation
radical, index, radicand	Use Properties of Inequalities
	Solve Linear Inequalities
	Solve Combined Inequalities
	Solve Absolute Value Inequalities
	Add, Subtract, Multiply, and Divide Complex Numbers
	Solve Quadratic Equations with a Negative Discriminant
	Translate Verbal Descriptions into Mathematical Expressions
	Solve Interest Problems
	Solve Mixture Problems
	Solve Uniform Motion Problems
	Solve Constant Rate Job Problems
	Work with nth Roots
	Simplify Radicals
	Rationalize Denominators
	Solve Radical Equations
	Simplify Expressions with Rational Exponents

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C tich	How can you determine what the graph of a function	Functions and Graphs	Determine whether a relation is a function	MST3-A2.A.37 MST3-A2.A.38	
-	looks like based on its equation?				
	equations	Functions	Find the value of a function	MST3-A2.A.39 MST3-A2.A.40	
		Basic Graphs			
	How can you identify a piece-wise function?	Properties of Functions	Find the domain of a function	MST3-A2.A.52 MST3-A2.A.50	
		Polynomial Functions	Turiction		
	How do asymptotes affect	Rational Root Theorem		MST3-A2.A.51	
	the graphs of functions?		Identify the graph of a function		
		<u>Vocabulary</u>			
	Why does the Rational Root Theorem help us when solving polynomial functions?	relation, function, domain, range, even function, odd function, local maxima, local minima, piecewise functions, polynomial	Determine Even and Odd functions from a graph Determine Even and Odd		
		functions, polynomial functions, zero, root, asymptotes, rational zeros, real zeros	function from the equation		
			Justify why a function is even or odd		
			Use a Graph to determine where a function is increasing, decreasing or constant		
			Use a Graph to locate local maxima and local minima		
			Graph Piecewise-defined functions		
			Identify polynomial functions and their degree		
			Identify zeros of polynomial functions		
			Analyze the graph of a polynomial function		
			Find the domain of a rational function		
			Find the vertical and horizontal asymptotes of a rational functions		

	Use the Remainder and Factor Theorems		
	Use the Rational Zeros Theorem		
	Explain why we use the Rational Zeros Theorem		
	Find the real zeros of a polynomial function		
	Solve polynomial equations		
	Find complex zeros of a polynomial		

	Essential Questions	Content	Skills	Assessments	Standards/PIs	Resources/Notes
Unit 4	How do exponential and logarithmic functions relate to the real world?	Exponential and Logarithmic Functions and Equations	Evaluate exponential functions	(MST3-A2.A.27 MST3-A2.A.28 MST3-A2.A.53	:
		Exponential Functions	Graph exponential functions		MST3-A2.A.54	
		Logarithmic Functions	Define the number e			
			Solve exponential equations			
		Growth and Decay Problems				
		<u>Vocabulary</u>	Change exponential expressions to logarithmic expressions and logarithmic expressions to exponential expressions			
		exponential function, e, natural logarithm function, common logarithm function, simple interest, compound interest formula, continuous compounding, present value	Evaluate logarithmic expressions			
			Determine the domain of a logarithmic function			
			Graph logarithmic functions			
			Solve logarithmic equations			
			Determine the future value of a lump sum of money			
			Calculate effective rates of return			
			Determine the present value of a lump sum of money			
			Determine the time required to double or triple a lump sum of money			
			Find equations of populations that obey the Law of Uninhibited Growth			
			Find equations of populations that obey the Law of Decay			

Unit 5	Why are matrices helpful in solving linear equations?	System of Linear Equations	Solve systems of equations by substitution		
	What is the purpose of a determinant?	Systems of Linear Equations: Substitution and Elimination	Solve systems of equations by elimination		
	How do matrices apply to business?	Matrices	Identify inconsistent systems of equations containing two variables		
		Determinants	Express the solution of a		
	Why do we decompose rational expressions into partial fractions?	Matrix Algebra	system of dependent equations containing two variables		
		Partial Fraction Decomposition	Solve systems of three equations containing three variables		
		<u>Vocabulary</u>	Identify inconsistent systems of equations containing three variables		
		consistent, inconsistent, independent, dependent, method of substitution, method of elimination, matrix, row index, column index, augmented matrix, coefficient matrix, row operations, row echlelon	Express the solution of a system of dependent equations containing three variables		
		form, determinant, Cramer's Rule, scalar, inverse, nonsingular, singular,	Write the augmented matrix of a system of linear equations		
			Write the system from the augmented matrix		
			Perform row operations on a matrix		
			Solve a system of linear equations using matrices		
			Evaluate 2 by 2 determinants		
			Use Cramer's Rule to solve a system of two equations containing two variables		

			Evaluate 3 by 3 determinants		
			Use Cramer's Rule to solve a system of three equations containing three variables		
			Know how to apply properties of determinants		
			Find the sum and difference of two matrices		
			Find scalar multiples of a matrix		
			Find the product of two matrices		
			Find the inverse of a matrix		
			Solve a system of linear equations using inverse matrices		
			Decompose P/Q, where Q has only nonrepeated linear factors		
			Decompose P/Q, where Q has repeated linear factors		
			Decompose P/Q, where Q has a nonrepeated irreducible quadratic factor		
			Decompose P/Q, where Q has repeated irreducible quadratic factor		
Unit 6	Why is polar graphing important?	Polar Coordinates	Plot points using polar coordinates	(
j	What are some applications of polar graphing?	Polar Coordinates	Convert from polar coordinates to rectangular		
		Polar Equations and Graphs	coordinates to rectangular coordinates		

	<u>Vocabulary</u>	Convert from rectangular coordinates to polar coordinates		
	polar grids, cardiod,	Graph and identify polar equations by converting to rectangular equations		
		Graph polar equations using a graphing utility		
		Graph polar equations by plotting points		

	Essential Questions	Content	Skills	Assessments	Standards/PIs	Resources/Notes
Unit 7	How can conic sections be applied in the real world?	Conic Sections	Work with circles with center at origin	(MST3-G.G.74 MST3-A2.A.47	
		The Circle	Work with circles with center at (h, k)		MST3-A2.A.24	
		The Ellipse				
		The Hyperbola	Convert from standard form to center-radius form			
		Vocabulary	Work with ellipses with center at the orgin			
		conic, ellipse, hyperbola, major axis, minor axis, vertices, foci, complete the square, asymptotes	Work with ellipses with center at (h, k)			
		oqualo, adymptotod	Solve applied problems involving ellipses			
			Work with hyperbolas with center at the origin			
			Find the asymptotes of a hyperbola			
			Work with hyperbolas with center at (h, k)			
			Solve applied problems involving hyperbolas			
Unit 8	How does the limit describe the nature of a function?	Intro to Calculus	Find the limit using a table	Ċ		
	What does the derivative tell us about the function?	Limits	Find the limit using a graph			
		Derivatives	Find the one-sided limits of a function			
		<u>Vocabulary</u>	Determine whether a function is continuous			
		limit, "as x approaches", derivative	Find the derivative using the limit definition			

	Apply the power rule		
	Apply the chain rule		
	Apply the product rule		
	Apply the quotient rule		
	Explain the difference between average rate change and instantaneous rate of change		

Key to Standards used in this Map

MST3-A2.N.6 [1 occurence] - MST Standard 3 - Number Sense and Operations Strand - Students will understand meanings of operations and procedures, and how they relate to one another. [Operations] - Performance Indicator A2.N.6 - write square roots of negative numbers in terms of i [Algebra 2 and Trigonometry]

MST3-A2.N.7 [1 occurence] - MST Standard 3 - Number Sense and Operations Strand - Students will understand meanings of operations and procedures, and how they relate to one another. [Operations] - Performance Indicator A2.N.7 - simplify powers of i [Algebra 2 and Trigonometry]

MST3-A2.N.9 [1 occurence] - MST Standard 3 - Number Sense and Operations Strand - Students will understand meanings of operations and procedures, and how they relate to one another. [Operations] - Performance Indicator A2.N.9 - perform arithmetic operations on complex numbers and write the answer in the form a + bi . [Algebra 2 and Trigonometry]

MST3-A2.A.7 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Variables and Expressions] - Performance Indicator A2.A.7 - factor polynomial expressions completely, using any combination of the following techniques: common factor extraction, difference of two perfect squares, quadratic trinomials [Algebra 2 and Trigonometry]

MST3-A2.A.8 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Variables and Expressions] - Performance Indicator A2.A.8 - apply the rules of exponents to simplify expressions involving negative and/or fractional exponents [Algebra 2 and Trigonometry]

MST3-A2.A.16 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Variables and Expressions] - Performance Indicator A2.A.16 - perform arithmetic operations with rational expressions and rename to lowest terms [Algebra 2 and Trigonometry]

MST3-A2.A.24 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Equations and Inequalities] - Performance Indicator A2.A.24 - know and apply the technique of completing the square [Algebra 2 and Trigonometry]

MST3-A2.A.25 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Equations and Inequalities] - Performance Indicator A2.A.25 - solve quadratic equations, using the quadratic formula [Algebra 2 and Trigonometry]

MST3-A2.A.26 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Equations and Inequalities] - Performance Indicator A2.A.26 - find the solution to polynomial equations of higher degree that can be solved using factoring and/or the quadratic formula [Algebra 2 and Trigonometry]

MST3-A2.A.27 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Equations and Inequalities] - Performance Indicator A2.A.27 - solve exponential equations with and without common bases [Algebra 2 and Trigonometry]

MST3-A2.A.28 [1 occurence] - MST Standard 3 - Algebra Strand - Students will perform algebraic procedures accurately. [Equations and Inequalities] - Performance Indicator A2.A.28 - solve a logarithmic equation by rewriting as an exponential equation [Algebra 2 and Trigonometry]

MST3-A2.A.37 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Patterns, Relations and Functions] - Performance Indicator A2.A.37 - define a relation and function [Algebra 2 and Trigonometry]

MST3-A2.A.38 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Patterns, Relations and Functions] - Performance Indicator A2.A.38 - determine when a relation is a function [Algebra 2 and Trigonometry]

MST3-A2.A.39 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Patterns, Relations and Functions] - Performance Indicator A2.A.39 - determine the domain and range of a function from its equation [Algebra 2 and Trigonometry]

MST3-A2.A.40 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Patterns, Relations and Functions] - Performance Indicator A2.A.40 - write functions in functional notation [Algebra 2 and Trigonometry]

MST3-A2.A.47 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.47 - determine the center-radius form for the equation of a circle in standard form [Algebra 2 and Trigonometry]

MST3-A2.A.50 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.50 - approximate the solution to polynomial equations of higher degree by inspecting the graph [Algebra 2 and Trigonometry]

MST3-A2.A.51 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.51 - determine the domain and range of a function from its graph [Algebra 2 and Trigonometry]

MST3-A2.A.52 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.52 - identify relations and functions, using graphs [Algebra 2 and Trigonometry]

MST3-A2.A.53 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.53 - graph exponential functions of the form y=bx for positive values of b, including b=e [Algebra 2 and Trigonometry]

MST3-A2.A.54 [1 occurence] - MST Standard 3 - Algebra Strand - Students will recognize, use, and represent algebraically patterns, relations, and functions. [Coordinate Geometry] - Performance Indicator A2.A.54 - graph logarithmic functions, using the inverse of the related exponential function [Algebra 2 and Trigonometry]

MST3-G.G.74 [1 occurrence] - MST Standard 3 - Geometry Strand - Students will apply coordinate geometry to analyze problem solving situations. [Coordinate Geometry] - Performance Indicator G.G.74 - graph circles of the form (x-h)2 + (j-k)2 = r2 [Geometry]